

Test 4: Newton's Laws II

2011

Equations and Constants:

$$\bar{v} = \frac{\Delta x}{\Delta t}$$

$$v = \frac{dx}{dt}$$

$$\bar{a} = \frac{\Delta v}{\Delta t}$$

$$a = \frac{dv}{dt}$$

$$\bar{v} = \frac{1}{2}(v_i + v_f)$$

$$|g| = 10 \text{ m/s}^2$$

$$x = \frac{1}{2}at^2 + v_i t + x_i$$

$$v = at + v_i$$

$$v_f^2 = v_i^2 + 2a\Delta x$$

$$R = \frac{v^2 \sin 2\theta}{g}$$

$$a_c = \frac{v^2}{r}$$

$$\sum \vec{F} = m\vec{a}$$

$$w = mg$$

$$w_{\perp} = mg \cos \theta$$

$$w_{\parallel} = mg \sin \theta$$

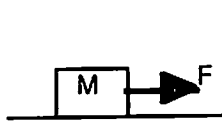
$$f = \mu N$$

**Multiple Choice:** Choose the letter of the best answer. 3 points each.

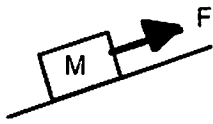
1. A A brick slides on a horizontal surface. Which of the following will increase the magnitude of the frictional force on it?
- Putting a second brick on top.
 - Decreasing the surface area of contact.
 - Increasing the surface area of contact.
 - Decreasing the mass of the brick.
 - None of the above.

2. C A 5 kg Jigglypuff is being pulled across the floor at a constant speed. The coefficient of friction between Jigglypuff and the floor is 0.3. What is the force of friction?
- 1.5 N.
 - 5 N.
 - 15 N.
 - 35 N.
 - 50 N.

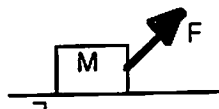
3. D In which of the following diagrams would the force of friction be the most?



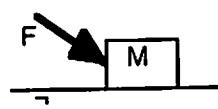
a.



b.



c.



d.

4. B An elephant and a mouse decide to go cliff diving in Mexico. While they are falling, who experiences the greater force of air resistance?
- the mouse.
 - the elephant.
 - they are always the same.
 - they are the same once they reach terminal speed.
 - at first the mouse, but then the elephant.

5. A What is meant by term "terminal speed?"
- It is the fastest you fall if only gravity is pulling you down.
 - It is the fastest you can ever travel through the air.
 - It is the fastest you can travel in an airport.
 - It is the speed that will kill you.

6. E The coefficient of kinetic friction:
- is in the direction of the frictional force
 - is in the direction of the normal force
 - is the ratio of force to area
 - can have units of newtons
 - is none of the above

7. B A forward horizontal force of 12 N is used to pull a 240-N crate at constant velocity across a horizontal floor. The coefficient of friction is:
- 0.5
 - 0.05
 - 2.0
 - 0.2
 - 20.0

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8. D An object moving in a circle at constant speed:
- must have only one force acting on it
 - is not accelerating
 - is held to its path by centrifugal force so that the net force is zero.
 - has an acceleration of constant magnitude
 - has an acceleration that is tangent to the circle
9. B Why do raindrops fall with constant speed during the later stages of their descent?
- The gravitational force is the same for all drops.
 - Air resistance just balances the force of gravity.
 - The drops all fall from the same height.
 - The force of gravity is negligible for objects as small as raindrops.
 - Gravity cannot increase the speed of a falling object to more than 9.8 m/s.

Questions 10 to 12 refer to the following:

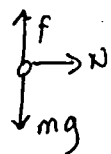
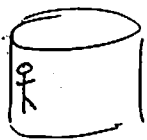
A person of mass m is riding a Ferris Wheel that rotates with a constant speed. The centripetal acceleration of the person is g .

10. E When the person is at the highest point of the ride, what is the normal force acting on the person?
- mg (up).
 - mg (down).
 - $2mg$ (down).
 - $2mg$ (up).
 - 0.
11. A When the person is at the lowest point of the ride, what is the net force on the person?
- mg (up).
 - mg (down).
 - $2mg$ (down).
 - $2mg$ (up).
 - 0.
12. D What would happen if the ride somehow doubled in speed?
- The person would be killed by the massive centripetal forces.
 - The ride would be a lot more "fun", but still certainly safe.
 - The ride would be especially dangerous at its lowest points because the person would be flung out of the ride at high speed.
 - There would not be enough gravity at the highest points of the ride to keep the person moving in a circle and so they would become a projectile.
13. A Pikachu ($m = 3$ kg) is asleep on the floor. Ash tries to pull Pikachu with a force of 7 N, but the Pokemon doesn't move. There is a coefficient of friction of 0.4. What is the force of friction on Pikachu?
- 7 N.
 - 12 N.
 - 18 N.
 - 23 N.
 - 30 N.
14. B Imagine trying to push a large object across the floor. Why does it usually take more force to get the object initially moving than it does to keep it moving with a constant speed?
- Because you are weak.
 - Because static friction can be stronger than kinetic friction.
 - Because there is a lot of inertia in the large object.
 - Because objects at rest want to stay at rest.
 - Because of Newton's Third Law.

Connor
Miss P
Miss A.
Mrs. Quinn
Ryan

Problem Solving: Show all work, including a correct free-body diagram.

15. Someone wants to design a "kinder and gentler" Turkish Twist ride. They would like it to have a 9 meter radius and rotate at only 4 rpm. What should be the minimum coefficient of friction on the walls so that the riders will stay suspended on the wall when the floor drops. Also make a brief comment on how feasible this ride is.



$$\sum F_x = \frac{mv^2}{r}$$

$$\sum F_y = 0$$

$$N = \frac{mv^2}{r}$$

$$f - mg = 0$$

$$f = \mu N$$

$$\therefore \mu \left(\frac{mv^2}{r} \right) = mg$$

$$\Rightarrow \mu = \frac{rg}{v^2}$$

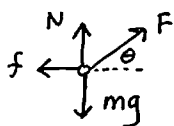
$$\left(4 \frac{\text{rev}}{\text{min}} \right) \left(\frac{1 \text{ min}}{60 \text{ s}} \right) \left(\frac{2\pi(9) \text{ m}}{1 \text{ rev}} \right) = \underline{3.77 \text{ m/s}}$$

$$\therefore \mu = \frac{(9)(10)}{(3.77)^2}$$

$$\mu = 6.3$$

hey! That's HUGE so won't work.

16. Starting from rest, a 7.5 kg mass is being dragged across a floor by a force of 40 N at an angle of 65° above the horizontal. The coefficient of friction is 0.4. How long will it take to drag the mass 6 meters?



$$\sum F_x = ma$$

$$\sum F_y = 0$$

$$F \cos \theta - f = ma$$

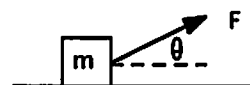
$$N + F \sin \theta - mg = 0$$

$$\therefore N = mg - F \sin \theta$$

$$F \cos \theta - \mu (mg - F \sin \theta) = ma$$

$$a = \frac{F \cos \theta - \mu (mg - F \sin \theta)}{m}$$

$$a = \frac{40 \cos 65 - 0.4[(7.5)(10) - (40 \sin 65)]}{7.5} = \underline{0.187 \text{ m/s}^2}$$



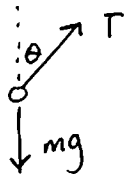
$$d = \frac{1}{2} at^2$$

$$6 = \frac{1}{2} (0.187) t^2$$

$$t^2 = 64$$

$$t = 8 \text{ s}$$

17. A conical pendulum is made from a mass of 150 grams connected to a string of length 1.2 meters. It is spinning such that the string makes a 35° angle from the vertical. What is the period of the motion?



$$\sum F_x = \frac{mv^2}{r}$$

$$\sum F_y = 0$$

$$T \sin \theta = \frac{mv^2}{r}$$

$$T \cos \theta - mg = 0$$

$$r = L \sin \theta$$

$$\frac{T \sin \theta}{T \cos \theta} = \frac{\frac{mv^2}{r}}{mg}$$

$$\tan \theta = \frac{v^2}{rg}$$

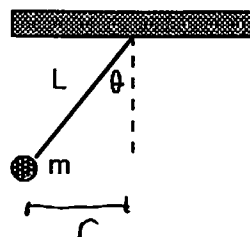
$$v^2 = rg \tan \theta = L \sin \theta g \tan \theta$$

$$= (1.2)(\sin 35)(10)(\tan 35)$$

$$v^2 = 4.82$$



$$v = \underline{2.2 \text{ m/s}}$$



$$v = \frac{2\pi r}{t}$$

$$t = \frac{2\pi r}{v} = \frac{2\pi (1.2) \sin 35}{2.2}$$

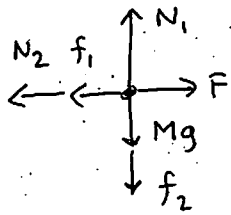
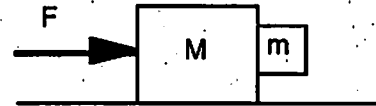
$$t = 1.97 \text{ s}$$

side 3

v.a

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18. A mass M is on a table with a coefficient of friction of μ_1 . It is being pushed by a horizontal force F . What must F be so that a mass m will stay suspended in front of M (as shown) if the coefficient of friction between the masses is μ_2 ?



$$\sum F_x = Ma$$

$$\sum F_y = 0$$

$$F - f_1 - N_2 = Ma$$

$$N_1 - Mg - f_2 = 0$$

$$f_1 = \mu_1 N_1$$

System:

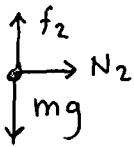
$$F - f_1 = (M+m)a$$

$$F - \mu_1(M+m)g = (M+m)a$$

$$F = \mu_1(M+m)g + (M+m)a$$

$$F = \mu_1(M+m)g + \frac{1}{\mu_2}(M+m)g$$

$$F = \left(\mu_1 + \frac{1}{\mu_2}\right)(M+m)g$$



$$\sum F_x = ma$$

$$\sum F_y = 0$$

$$N_2 = ma$$

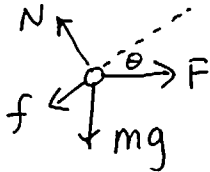
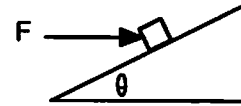
$$f_2 - mg = 0$$

$$f_2 = \mu_2 N_2$$

$$\therefore f_2 = mg = \mu_2 N_2 = \mu_2 ma$$

$$\therefore a = \frac{g}{\mu_2}$$

19. An object of mass m is pushed up a hill at constant speed. The base angle of the hill is θ and the minimum force needed to keep it moving up the hill is F (directed horizontally, as shown.) What is the coefficient of friction?



$$\sum \vec{F} = 0$$

$$\sum F_{||} = 0$$

$$\sum F_{\perp} = 0$$

$$F \cos \theta - f - mg \sin \theta = 0$$

$$N - mg \cos \theta - F \sin \theta = 0$$

$$\rightarrow N = mg \cos \theta + F \sin \theta$$

$$f = \mu N$$

$$F \cos \theta - \mu (mg \cos \theta + F \sin \theta) - mg \sin \theta = 0$$

$$\mu (mg \cos \theta + F \sin \theta) = F \cos \theta - mg \sin \theta$$

$$\mu = \frac{F \cos \theta - mg \sin \theta}{mg \cos \theta + F \sin \theta}$$